

Calc II - A few probability problems

1. Use u -substitution to translate the following normal integral into a standard normal integral:

$$\frac{1}{\sqrt{2\pi} \cdot 3} \int_0^4 e^{-(x-1)^2/18} dx.$$

2. I've got an unfair coin that comes up heads $3/5$ of the time. Suppose I flip that coin 500 times, count the number of heads I get, and call that value S .
- Find $E(S)$ - i.e. the mean or expectation of S .
 - Find $\sigma^2(S)$ and $\sigma(S)$ - i.e. the variance and standard deviation of S
 - Write down a normal integral that represents $P(290 < S < 320)$.
3. I've got a 10 sided die with
- Three sides labeled 1,
 - four sides labeled 2, and
 - three sides labeled 3.

Let X denote the numerical value of 1 roll and let S the sum of the numerical values of 300 rolls.

- Find $E(X)$ and $\sigma(X)$.
- Find $E(S)$ and $\sigma(S)$.
- Write down a normal integral representing $P(S > 595)$