## Review for quiz 1

2025-08-22

We have our first quiz next Friday, August 29th. This problem sheet represents most of the problems that will be on the quiz, though, I might add a problem after Monday's class.

## **Problems**

1. Curious about the following limit,

$$\lim_{x\to 0} (1+x)^{3/x},$$

I used my computer to plug in several values of x that are *close* to 0 but not equal to 0. The results are shown in Table 1 below.

Table 1: Values of  $f(x) = (1+x)^{3/x}$  near x = 0.

x	0.100000	0.010000	0.001000	0.000100	0.000010
f(x)	17.449402	19.788466	20.055451	20.082525	20.085236

Based on those computations, can you make a conjecture as to the approximate value of the limit? Be sure to indicate how many digits you believe to be correct and why.

2. The graph of

$$f(x) = \frac{x-1}{x^3 - x^2 + x - 1}$$

is shown in Figure 1.

- a) Judging from the figure, what do you suppose is the value of  $\lim_{x\to 1} f(x)$ ?
- b) Use a little algebra together with the limit laws to prove that your guess is correct.
- 3. The Complete graph of a function f is shown in Figure 2. At each of the points a=-1, a=1, a=2 and a=4, find the value of
  - a) f(a),

b) 
$$\lim_{x\to a^-} f(x)$$

$$\begin{array}{ll} \text{b)} & \lim_{x \to a^-} f(x), \\ \text{c)} & \lim_{x \to a^+} f(x), \text{ and} \\ \text{d)} & \lim_{x \to a} f(x). \end{array}$$

d) 
$$\lim_{x\to a} f(x)$$

## 4. Compute the following limits.

a) 
$$\lim_{x\to 2} \frac{2x^2-3x-2}{x-2}$$
 b)  $\lim_{x\to 1} \frac{x-2}{x^3+x-2}$ 

b) 
$$\lim_{x \to 1} \frac{x-1}{x^3 + x - 2}$$

## **Figures**

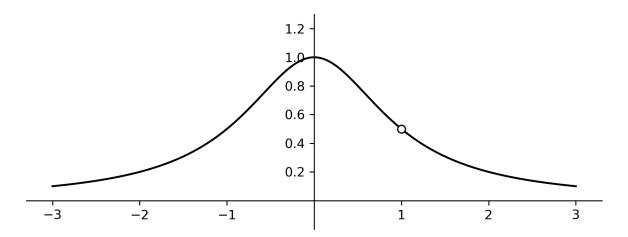


Figure 1: The graph of  $f(x)=(x-1)/(x^3-x^2+x-1)$ 

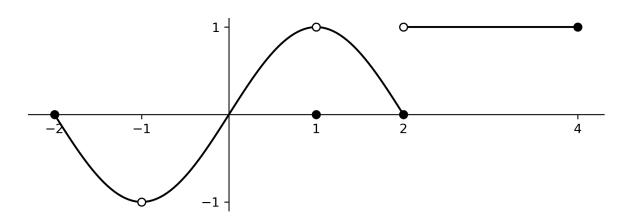


Figure 2: A graph for limits