Calc II Problem sheet

Thursday, July 8

1. Write down a couple of complete sentences using the comparison test to show that

$$\sum_{n=1}^{\infty} \frac{\sin\left(n^3\right)}{n^4}$$

converges absolutely.

2. Write down a couple complete sentences using the alternating series test to show that

$$\sum_{n=1}^{\infty} (-1)^{n+1} \frac{\ln(n)}{n}$$

converges conditionally.

3. Suppose we'd like to approximate

$$\sum_{n=1}^{\infty} (-1)^{n+1} \frac{n}{n^2 + 1}$$

by truncating the sum to obtain a finite sum of the form

$$\sum_{n=1}^{N} (-1)^{n+1} \frac{n}{n^2 + 1}.$$

How large does N have to be to ensure that our approximation is within 0.0001 of the actual value?